

- (24) $\tan x$ (25) 2 (26) 1 (27) $\sec x$ (29) $\tan x$ (30) $\cos y$
 (31) $\tan x$ (32) $\sin x$ (33) $2\csc^2 x$ (35) $-\sin x$ (37) $\cot x$

SOLUTIONS

$$(24) \frac{1 + \tan x}{1 + \cot x} = \frac{\frac{\cos x}{\cos x} + \frac{\sin x}{\cos x}}{\frac{\sin x}{\sin x} + \frac{\cos x}{\sin x}} = \frac{\frac{\cos x + \sin x}{\cos x}}{\frac{\sin x + \cos x}{\sin x}} = \frac{\cos x + \sin x}{\cos x} \cdot \frac{\sin x}{\sin x + \cos x} = \frac{\sin x}{\cos x} = \boxed{\tan x}$$

$$(25) \frac{(\sec^2 x + \csc^2 x) - (\tan^2 x + \cot^2 x)}{\sec^2 x + \csc^2 x - \tan^2 x - \cot^2 x} = \frac{\sec^2 x - \tan^2 x + \csc^2 x - \cot^2 x}{\sec^2 x - \tan^2 x + \csc^2 x - \cot^2 x} = \frac{1 + 1}{1 + 1} = \boxed{2}$$

$$(26) \frac{\sec^2 u - \tan^2 u}{\cos^2 v + \sin^2 v} = \frac{1}{1} = \boxed{1}$$

$$(27) \frac{\sin x (\tan x + \cot x)}{\sin x \tan x + \sin x \cot x} = \frac{\sin x \cdot \frac{\sin x}{\cos x} + \sin x \cdot \frac{\cos x}{\sin x}}{\frac{\sin^2 x}{\cos x} + \frac{\cos^2 x}{\sin x}} = \frac{\frac{\sin^2 x}{\cos x} + \frac{\cos^2 x}{\sin x}}{\frac{\sin^2 x}{\cos x} + \frac{\cos^2 x}{\sin x}} = \frac{1}{\cos x} = \boxed{\sec x}$$

$$(29) \frac{\cancel{\sin x} \cdot \cancel{\cos x} \cdot \sin x \cdot \frac{1}{\cancel{\cos x}} \cdot \frac{1}{\cancel{\sin x}}}{\cancel{\cos x} \cdot \cancel{\sin x}} = \frac{\sin x}{\cos x} = \boxed{\tan x}$$

$$(30) \frac{\sec^2 y - \tan^2 y}{\sec y} = \frac{1}{\sec y} = \boxed{\cos y}$$

$$(31) \tan x \cdot \frac{1}{\csc^2 x} + \tan x \cdot \frac{1}{\sec^2 x} = \tan x \cdot \sin^2 x + \tan x \cdot \cos^2 x = \tan x (\sin^2 x + \cos^2 x) = \boxed{\tan x}$$

$$(32) \frac{\sec^2 x \csc x}{\csc^2 x \sin x} = \frac{1}{\cos^2 x} \cdot \frac{1}{\sin x} = \frac{1}{\cos^2 x \sin x} = \frac{1}{\csc^2 x \sin x}$$

$$\begin{aligned} (32) \quad \frac{\sec^2 x \csc x}{\sec^2 x + \csc^2 x} &= \frac{\frac{1}{\cos^2 x} \cdot \frac{1}{\sin x}}{\frac{\sin^2 x}{\sin^2 x} \frac{1}{\cos^2 x} + \frac{1}{\sin^2 x} \frac{\cos^2 x}{\cos^2 x}} = \frac{\frac{1}{\cos^2 x \sin x}}{\frac{\sin^2 x + \cos^2 x}{\cos^2 x \sin^2 x}} = \frac{1}{\cos^2 x \sin x} \cdot \frac{\cos^2 x \sin^2 x}{\sin^2 x + \cos^2 x} \\ &= \frac{1}{\cos^2 x \sin x} \cdot \frac{\cos^2 x \sin^2 x}{1} \\ &= \boxed{\sin x} \end{aligned}$$

$$\begin{aligned} (33) \quad \frac{1}{\sin^2 x} + \sec^2 x \cdot \cot^2 x &= \frac{1}{\sin^2 x} + \frac{1}{\cos^2 x} \cdot \frac{\cos^2 x}{\sin^2 x} = \frac{1}{\sin^2 x} + \frac{1}{\sin^2 x} = \frac{2}{\sin^2 x} \\ &= \boxed{2 \csc^2 x} \end{aligned}$$

$$\begin{aligned} (35) \quad \frac{\sin x}{\cot^2 x} - \frac{\sin x}{\cos^2 x} &= \sin x \cdot \frac{1}{\cot^2 x} - \frac{\sin x}{\cos^2 x} = \sin x \cdot \frac{\sin^2 x}{\cos^2 x} - \frac{\sin x}{\cos^2 x} \\ &= \frac{\sin^3 x - \sin x}{\cos^2 x} = \frac{\sin x (\sin^2 x - 1)}{\cos^2 x} \\ &= \frac{\sin x (-\cancel{\cos^2 x})}{\cancel{\cos^2 x}} \\ &= \boxed{-\sin x} \end{aligned}$$

$$\begin{aligned} (37) \quad \frac{\sec x}{\sin x} - \frac{\sin x}{\cos x} &= \sec x \cdot \frac{1}{\sin x} - \frac{\sin x}{\cos x} = \frac{1}{\cos x} \cdot \frac{1}{\sin x} - \frac{\sin x \sin x}{\cos x \sin x} \\ &= \frac{1 - \sin^2 x}{\cos x \sin x} = \frac{\cancel{\cos^2 x}}{\cancel{\cos x} \sin x} = \boxed{\cot x} \end{aligned}$$