

A few more things to practice...

Writing Fractions in Reduced Form

$$\textcircled{1} \frac{1}{x} + 2 \cdot \frac{x}{x} = \frac{1}{x} + \frac{2x}{x} = \boxed{\frac{1+2x}{x}}$$

$$\textcircled{2} \frac{x(x+y)}{x-y(x+y)} \cdot \frac{y(x-y)}{x+y(x-y)} = \frac{x(x+y) - y(x-y)}{(x+y)(x-y)(x+y)(x-y)} = \frac{x^2 + xy - xy + y^2}{x^2y - y^2} = \boxed{\frac{x^2 + y^2}{x^2 - y^2}}$$

$$\textcircled{3} \frac{x^2 - y^2}{2xy} \div \frac{y^2 - x^2}{4x^2y} = \frac{(x+y)(x-y)}{2xy} \cdot \frac{4x^2y}{(y-x)(y+x)} = \frac{2x(x-y)}{-(x-y)} = \boxed{-2x}$$

Simplifying Compound Fractions

$$\textcircled{1} \frac{x+y}{\frac{y}{y} \cdot \frac{1}{x} + \frac{1}{y} \cdot \frac{x}{x}} = \frac{x+y}{1} \div \frac{y+x}{xy} = \frac{x+y}{1} \cdot \frac{xy}{y+x} = \boxed{xy}$$

$$\textcircled{2} \frac{\frac{b}{b} \cdot \frac{1}{a} + \frac{1}{b} \cdot \frac{a}{a}}{\frac{b}{b} \cdot \frac{a}{a} - \frac{a}{b} \cdot \frac{b}{a}} = \frac{\frac{b+a}{ab}}{\frac{b^2 - a^2}{ab}} = \frac{b+a}{ab} \cdot \frac{ab}{(b-a)(b+a)} = \boxed{\frac{1}{b-a}}$$

$$\textcircled{3} \frac{\frac{x+5}{x+5} \cdot 2 - \frac{12}{x+5}}{\frac{x-3}{x-3} \cdot 2 + \frac{3}{x-3}} = \frac{2(x+5) - 12}{x+5} \div \frac{2(x-3) + 3}{x-3} = \frac{2x-2}{x+5} \cdot \frac{x-3}{2x-3} = \frac{(2x-2)(x-3)}{(x+5)(2x-3)} = \boxed{\frac{2x^2 - 8x + 6}{2x^2 + 7x - 15}}$$