

- p. 425: 2, 8, 50, 51, 54
- p. 432: 2, 4, 12, 15, 16

② $\frac{3-\sqrt{3}}{3+\sqrt{3}}$

⑤ $\frac{-\sqrt{3}+1}{1+\sqrt{3}}$

⑤⑩ $\sin 3U = 3\cos^2 U \sin U - \sin^3 U$ ✓

$$\begin{aligned} & \sin(2U+U) \\ & \sin 2U \cos U + \cos 2U \sin U \\ & \sin(U+U) \cos U + \cos(U+U) \sin U \\ & (\sin U \cos U + \cos U \sin U) \cos U + (\cos U \cos U - \sin U \sin U) \sin U \\ & \sin U \cos^2 U + \sin U \cos^2 U + \sin U \cos^2 U - \sin^3 U \\ & 3\cos^2 U \sin U - \sin^3 U \checkmark \end{aligned}$$

⑤① $\cos 3x + \cos x = 2\cos 2x \cos x$ ✓

$$\begin{aligned} & \cos(2x+x) + \cos(2x-x) \\ & \cos 2x \cos x - \sin 2x \sin x + \cos 2x \cos x + \sin 2x \sin x \\ & 2\cos 2x \cos x \checkmark \end{aligned}$$

⑤④ $\tan 5u \tan 3u = \frac{\tan^2 4u - \tan^2 u}{1 - \tan^2 4u \tan^2 u}$ ✓

$$\begin{aligned} & \tan(4u+u) \tan(4u-u) \\ & \frac{\tan 4u + \tan u}{1 - \tan 4u \tan u} \frac{\tan 4u - \tan u}{1 + \tan 4u \tan u} \quad (\text{foil numerator \& denominator!}) \\ & \frac{\tan^2 4u - \tan^2 u}{1 - \tan^2 4u \tan^2 u} \checkmark \end{aligned}$$

② $\cos 2u = 2\cos^2 u - 1$ ✓

$$\begin{aligned} & \cos(u+u) \\ & \cos u \cos u - \sin u \sin u \\ & \cos^2 u - \sin^2 u \\ & \cos^2 u - (1 - \cos^2 u) \\ & \cos^2 u - 1 + \cos^2 u \\ & 2\cos^2 u - 1 \checkmark \end{aligned}$$

④ $\tan 2u = \frac{2\tan u}{1 - \tan^2 u}$ ✓

$$\begin{aligned} & \tan(u+u) \\ & \frac{\tan u + \tan u}{1 - \tan u \tan u} \\ & \frac{2\tan u}{1 - \tan^2 u} \checkmark \end{aligned}$$

⑫ $\sin 2\theta + \cos 2\theta$
 $\sin(\theta+\theta) + \cos(\theta+\theta)$
 $\sin\theta \cos\theta + \sin\theta \cos\theta + \cos^2\theta - \sin^2\theta$
 $\boxed{2\sin\theta \cos\theta} \quad \underbrace{\cos^2\theta - \sin^2\theta}_{=1}$

⑮ $\sin 4x = 2\sin 2x \cos 2x$ ✓

$$\begin{aligned} & \sin(2x+2x) \\ & \sin 2x \cos 2x + \cos 2x \sin 2x \\ & 2\sin 2x \cos 2x \checkmark \end{aligned}$$

⑯ $\cos 6x = 2\cos^2 3x - 1$ ✓

$$\begin{aligned} & \cos(3x+3x) \\ & \cos 3x \cos 3x - \sin 3x \sin 3x \\ & \cos^2 3x - \sin^2 3x \\ & \cos^2 3x - (1 - \cos^2 3x) \\ & \cos^2 3x - 1 + \cos^2 3x \\ & 2\cos^2 3x - 1 \checkmark \end{aligned}$$