

Notes Key

Monday, February 22, 2016 8:12 AM

Tips ① Get "sin x" and "cos x"

$\sin(-x) = -\sin x$ ② $\cos^2 x + \sin^2 x = 1$

③ Know your Trig Identities!

① $\frac{1}{1 - \sin x} + \frac{1}{1 + \sin x} = \frac{1 + \sin x}{(1 - \sin x)(1 + \sin x)} + \frac{1 - \sin x}{(1 + \sin x)(1 - \sin x)} = \frac{1}{1 - \sin^2 x} + \frac{1}{1 - \sin^2 x} = \frac{2}{1 - \sin^2 x} = \frac{2}{\cos^2 x} = 2 \sec^2 x$

$\frac{1 + \cancel{\sin x} + 1 - \cancel{\sin x}}{(1 - \sin x)(1 + \sin x)} = \frac{2}{1 - \sin^2 x} = \frac{2}{\cos^2 x} = 2 \sec^2 x$

② $\frac{\sin x}{1 - \cos x} + \frac{1 - \cos x}{\sin x}$

$\frac{\sin^2 x + (1 - \cos x)(1 - \cos x)}{(1 - \cos x)(\sin x)} = \frac{\sin^2 x + 1 - 2\cos x + \cos^2 x}{(1 - \cos x)(\sin x)} = \frac{2 - 2\cos x}{(1 - \cos x)(\sin x)} = \frac{2(1 - \cos x)}{(1 - \cos x)\sin x} = \frac{2}{\sin x}$

③ $\frac{1 + \cos x}{\sin x} = \frac{1}{\sin x} + \frac{\cos x}{\sin x}$

$= \boxed{\csc x + \cot x}$