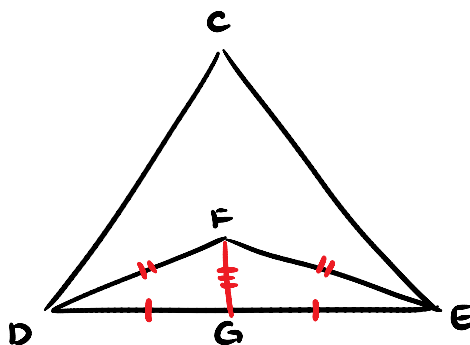


#11 Given: \overrightarrow{DF} bisects $\angle CDE$
 \overrightarrow{EF} bisects $\angle CED$
 G is the midpt of \overline{DE}
 $\overline{DF} \cong \overline{EF}$

Prove: $\angle CDE \cong \angle CED$



Statements

Reasons

- | | |
|---|--|
| 1. \overrightarrow{DF} bisects $\angle CDE$ | 1. Given |
| 2. \overrightarrow{EF} bisects $\angle CED$ | 2. Given |
| 3. G is the midpt of \overline{DE} | 3. Given |
| 4. $\overline{DG} \cong \overline{GE}$ (C) | 4. If a pt is a <u>midpt</u> \rightarrow divides the seg. into <u>2 \cong segs</u> |
| 5. $\overline{DF} \cong \overline{EF}$ (C) | 5. Given |
| 6. Draw \overline{FG} | 6. 2 pts determine a line |
| 7. $\overline{FG} \cong \overline{FG}$ (C) | 7. Reflexive prop |
| 8. $\triangle DFG \cong \triangle EFG$ | 8. SSS (4, 5, 7) |
| 9. $\angle FDG \cong \angle FEG$ | 9. CPCTC |
| 10. $\angle CDE \cong \angle CED$ | 10. If 2 \angle s are $\cong \rightarrow$ their like multiples are \cong
(If $2 \angle$ s $\times 2 \rightarrow$ products \cong) |

#14 Given: $\odot O$ and $\odot P$
 Perimeter of $\triangle AOP = 80$
 $OC + DP = 16$
 \overline{CD} is 2 units longer than \overline{OC}

$$AO + AP + OC + CD + DP = \text{Perimeter of } \triangle AOP$$

$$\text{Let } OC = x$$

$$DP = 16 - x$$

$$CD = x + 2$$

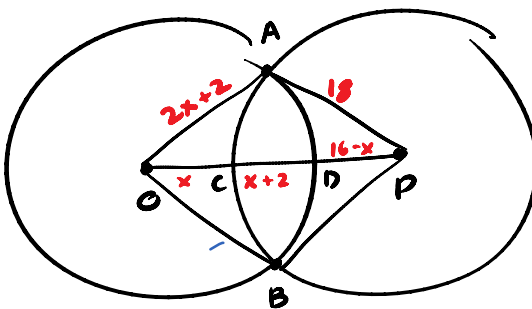
$$\text{because all radii are } \cong \quad OD = OA = x + x + 2 = 2x + 2$$

$$PC = PA = x + 2 + 16 - x = 18$$

$$\begin{aligned} x + x + 2 + 16 - x + 18 + 2x + 2 &= 80 \\ 3x + 38 &= 80 \\ 3x &= 42 \\ x &= 14 \end{aligned}$$

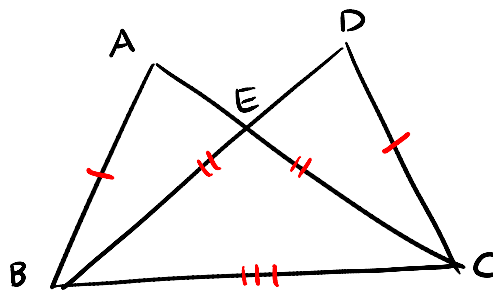
$$\begin{aligned} OB &= 30 \\ BP &= 18 \end{aligned}$$

$$\begin{aligned} OB + BP &= 30 + 18 \\ &= \boxed{48} \end{aligned}$$



#1 Given: $\overline{AB} \cong \overline{DC}$
 $\overline{AC} \cong \overline{DB}$

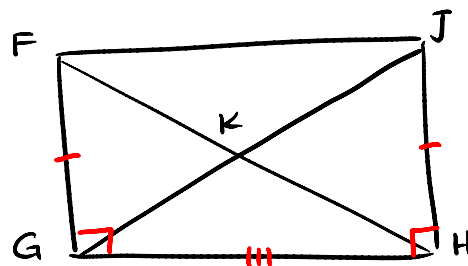
Prove: $\triangle ABC \cong \triangle DCB$



Statements	Reasons
1.) $\overline{AB} \cong \overline{DC}$ (S)	1.) Given
2.) $\overline{AC} \cong \overline{DB}$ (S)	2.) Given
3.) $\overline{BC} \cong \overline{BC}$ (S)	3.) Reflexive property
4.) $\triangle ABC \cong \triangle DCB$	4.) SSS (1, 2, 3)

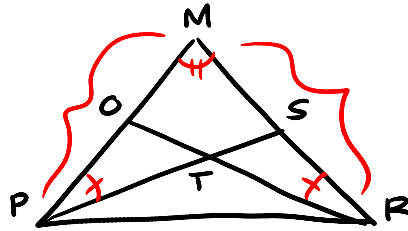
#2 Given: $\angle FGH$ is a right \angle
 $\angle JHG$ is a right \angle
 $\overline{FG} \cong \overline{JH}$

Prove: $\triangle FGH \cong \triangle JHG$



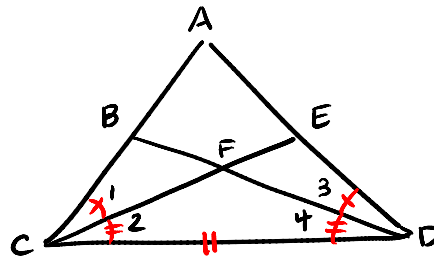
Statements	Reasons
1.) $\angle FGH$ is a right \angle	1.) Given
2.) $\angle JHG$ is a right \angle	2.) Given
3.) $\angle FGH \cong \angle JHG$ (A)	3.) If 2 \angle 's are right \angle 's $\rightarrow \angle$'s \cong
4.) $\overline{FG} \cong \overline{JH}$ (S)	4.) Given
5.) $\overline{GH} \cong \overline{GH}$ (S)	5.) Reflexive property
6.) $\triangle FGH \cong \triangle JHG$	6.) SAS (4, 3, 5)

#3 Given: $\overline{PM} \cong \overline{RM}$
 $\angle SPM \cong \angle ORM$
 Prove: $\triangle PSM \cong \triangle ROM$



Statements	Reasons
1.) $\overline{PM} \cong \overline{RM}$ [S]	1.) Given
2.) $\angle SPM \cong \angle ORM$ [A]	2.) Given
3.) $\angle M \cong \angle M$ [A]	3.) Reflexive property
4.) $\triangle PSM \cong \triangle ROM$	4.) ASA (2, 1, 3)

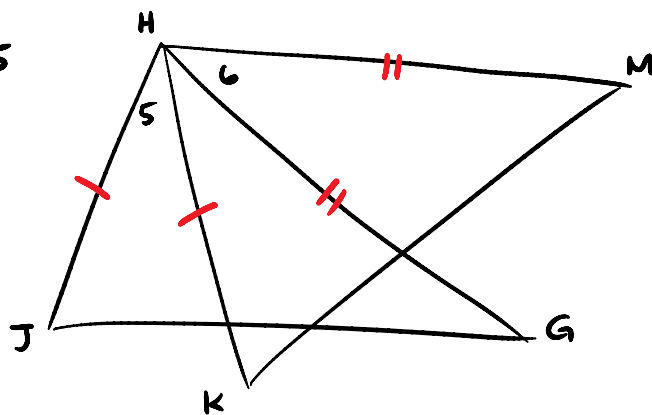
#4 Given: $\angle 1 \cong \angle 3$
 $\angle 2 \cong \angle 4$
 Conclusion: $\overline{BC} \cong \overline{ED}$



Statements	Reasons
1.) $\angle 1 \cong \angle 3$	1.) Given
2.) $\angle 2 \cong \angle 4$ [A]	2.) Given
3.) $\angle BCD \cong \angle EDC$ [A]	3.) Addition property
4.) $\overline{CD} \cong \overline{CD}$ [S]	4.) Reflexive property
5.) $\triangle BCD \cong \triangle EDC$	5.) ASA (2, 4, 3)
6.) $\overline{BC} \cong \overline{ED}$	6.) CPCTC

↙ If $2 \cong x's + 2 \cong x's \rightarrow Sums \cong$.

#5



Given: $\overline{JH} \cong \overline{KM}$
 $\overline{HG} \cong \overline{HM}$
 $\angle 5 \cong \angle 6$

Conc: $\triangle JHG \cong \triangle KHM$

Statements

Reasons

1. $\overline{JH} \cong \overline{KM}$ [S]
2. $\overline{HG} \cong \overline{HM}$ [S]
3. $\angle 5 \cong \angle 6$
4. $\triangle JHG \cong \triangle KHM$ [A]
5. $\triangle JHG \cong \triangle KHM$

1. Given
2. Given
3. Given
4. If the same \angle is added to $\cong \angle$'s
 \rightarrow sums are \cong
5. SAS (1, 4, 2)