

2.3 Graphing Polynomials

Zeros

x-int $(-, 0) \Rightarrow$ Real zeros } "Add" up to highest degree.
Imaginary zeros }

Multiplicity: How many times a zero appears in a function

Even \Rightarrow Kisses x-axis

ODD \Rightarrow Goes through.

Y-intercepts

$(0, -)$ \Rightarrow plug zero in for x.

Where the graph crosses y-axis

End behavior

$\lim_{x \rightarrow \infty} \Rightarrow \lim_{x \rightarrow R}$

$\lim_{x \rightarrow -\infty} \Rightarrow \lim_{x \rightarrow L}$

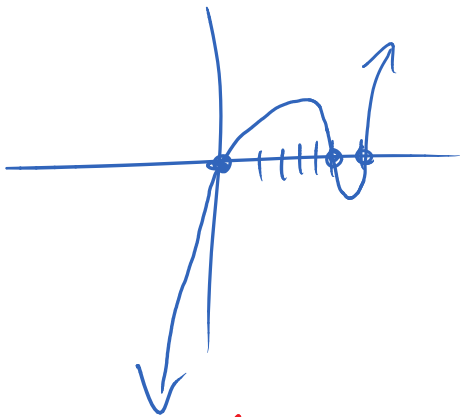
Even Degree \Rightarrow The left and right end behavior are the same

ODD Degree \Rightarrow The L. and R. End Behavior are opposite.

$$f(x) = x^3 - 11x^2 + 30x$$

$$0 = x(x-6)(x-5)$$

y-int: (0,0) $x=0, 6, 5$



$$\lim_{x \rightarrow \infty} = \infty$$

$$\lim_{x \rightarrow -\infty} = -\infty$$

$$g(x) = -2x^3(x-2)^2(2x-10)^2$$

$$0 = -2x^{\textcircled{3}}(x-2)^{\textcircled{2}}(2x-10)^{\textcircled{2}}$$

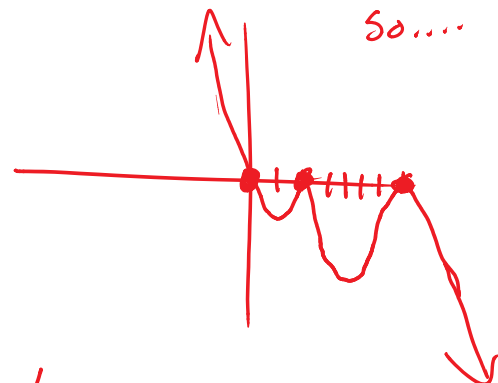
y-int: (0,0) $x=0, 2, 5$

Kiss the x-axis

$$-2x^3(x^2)(2x)^2 = -8x^7$$

Leading terms

So...



$$\lim_{x \rightarrow \infty} = -\infty$$

$$\lim_{x \rightarrow -\infty} = \infty$$