

#3 Find the center, the radius, the diameter, the circumference, and area of the circle

a.  $x^2 + y^2 = 36$

Center:  $(0,0)$

Radius: 6

Diam: 12

$C = 2\pi(6) = 12\pi$

$A = 36\pi$

b.  $(x-3)^2 + (y+6)^2 = 100$

Center:  $(3, -6)$

Radius: 10

Diam: 20

$C = 2\pi(10) = 20\pi$

$A = 100\pi$

c.  $(x+5)^2 + y^2 = \frac{9}{4}$

Center:  $(-5, 0)$

Radius:  $\frac{3}{2}$

Diameter: 3

$C = 2\pi\left(\frac{3}{2}\right) = 3\pi$

$A = \frac{9}{4}\pi$

d.  $\frac{(x+5)^2}{3} + \frac{(y-2)^2}{3} = 27$

$(x+5)^2 + (y-2)^2 = 81$

Center:  $(-5, 2)$

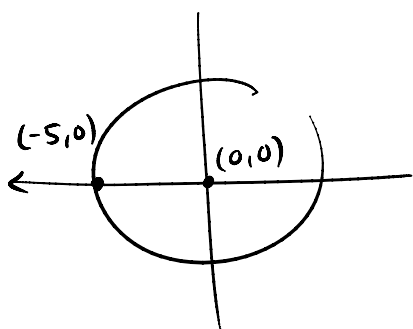
radius: 9

diameter

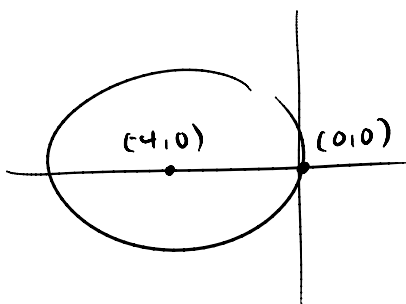
$C = 8\pi$

$A = 81\pi$

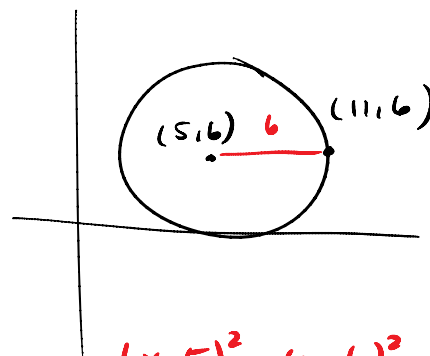
#4 Write equation of circle



$x^2 + y^2 = 25$



$(x+4)^2 + y^2 = 16$



$(x-5)^2 + (y-6)^2 = 36$

#5 Consider the equation  $(x-3)^2 + (y+2)^2 = 17$

a. Is  $(4,2)$  on the graph

$$\begin{aligned}(4-3)^2 + (2+2)^2 &= 17 \\ 1^2 + 4^2 &= 17 \\ 17 &= 17 \text{ yes}\end{aligned}$$

b. Is  $(3,-2)$  on the graph

$$\begin{aligned}(3-3)^2 + (-2+2)^2 &= 17 \\ 0^2 + 0^2 &= 17 \\ 0 &\neq 17 \text{ No}\end{aligned}$$

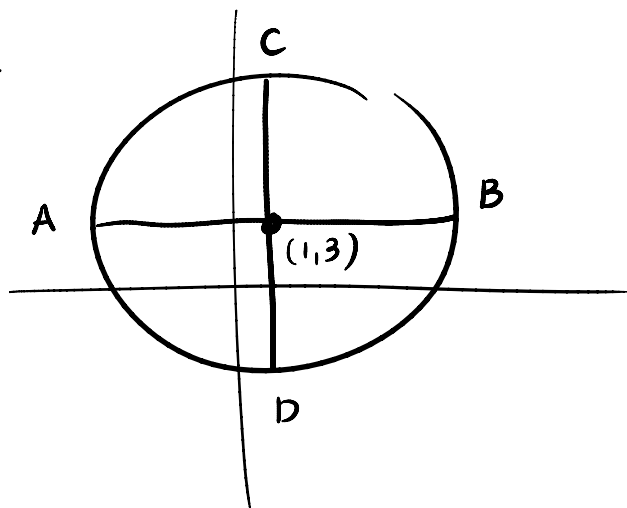
#6 a.  $(x-3)^2 + (y+1)^2 = 0$

Point Circle

b.  $(x+5)^2 + y^2 = -100$

Imaginary Circle

#7



#8 Determine the equation of each circle

a. The center is the origin, and the circle passes through  $(0, -5)$

$$x^2 + y^2 = 25$$

b. The endpoints of a diameter  $(-2, 1)$  and  $(8, 25)$

$$(x-3)^2 + (y-13)^2 = 169$$

c. The center is  $(-1, 7)$  and the circle passes through the origin

$$(x+1)^2 + (y-7)^2 = 50$$

d. The center is  $(2, -3)$  and the circle passes through  $(3, 0)$ .

$$(x-2)^2 + (y+3)^2 = 10$$

#9 Indicate whether the point is inside, on, or outside the circle.

a.  $(2, 5); x^2 + y^2 = 29$   
 $2^2 + 5^2 = 29$   
 $29 = 29 \checkmark$   
ON

b.  $(3, 0) \quad x^2 + y^2 = 100$   
 $(3)^2 + (0)^2 < 100$   
 $9 < 100$   
inside

c. Origin:  $(x-2)^2 + (y+5)^2 = 16$   
 $(-2)^2 + (5)^2 > 16$   
 $4 + 25 > 16$   
 $29 > 16$  outside

d.  $(-2, 1) \quad x^2 + (y+6)^2 = 23$   
 $(-2)^2 + (1+6)^2 = 23$   
 $4 + 7^2 = 23$   
 $53 = 23$  outside

#13 Find the distance between the points of intersection of the graph of  $x^2 + y^2 = 17$  and  $x + y = 3$

$$\begin{aligned}x^2 + (3-x)^2 &= 17 \\x^2 + 9 - 6x + x^2 &= 17 \\2x^2 - 6x - 8 &= 0 \\2(x^2 - 3x - 4) &= 0 \\2(x-4)(x+1) &= 0 \\x &= 4, -1\end{aligned}$$

points  $(4, -1)$   
 $(-1, 4)$

$$\begin{aligned}d &= \sqrt{(4+1)^2 + (4+1)^2} \\d &= \sqrt{5^2 + 5^2} \\d &= \sqrt{50} \\d &= 5\sqrt{2}\end{aligned}$$

#14

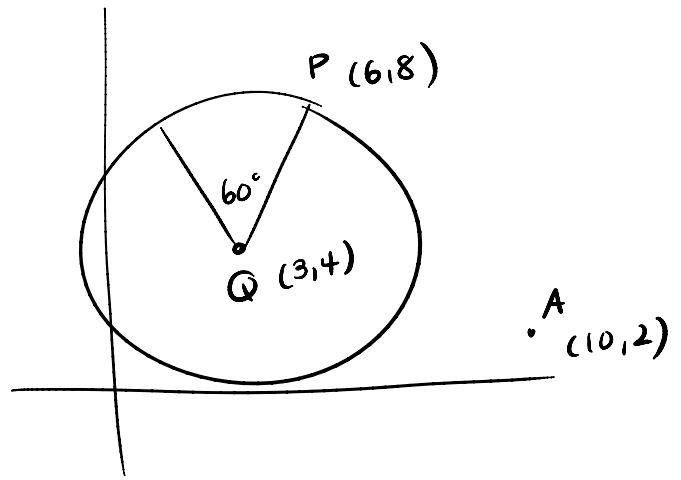
a. Equation of tangent to circle at (6,8)

$$m_{PQ} = \frac{8-4}{6-3} = \frac{4}{3}$$

(6,8)  
(3,4)

$$\perp m = -\frac{3}{4}$$

$$y - 8 = -\frac{3}{4}(x - 6)$$



b. Circumference

$$d = \sqrt{(8-4)^2 + (6-3)^2}$$

$$C = 10\pi$$

$$d = \sqrt{4^2 + 3^2}$$

$$d = \sqrt{16 + 9}$$

$$d = \sqrt{25}$$

$$d = 5$$

c. Dist  $\overline{AQ}$ 

$$\sqrt{53}$$

d. Distance from A to circle

$$\sqrt{53} - 5 \approx 2.3$$

e. Area of shaded sector

$$\frac{1}{6} \cdot \pi (5)^2 \approx 13.1$$